

A NEW TEST OF LORENTZ INVARIANCE VIOLATION: THE SPECTRAL LAG TRANSITION OF GRB 160625B

JUN-JIE WEI^{1,2}, BIN-BIN ZHANG^{3,4}, LANG SHAO^{5,1}, XUE-FENG WU^{1,6,7}, AND PETER MÉSZÁROS^{8,9,10}

¹Purple Mountain Observatory, Chinese Academy of Sciences, Nanjing 210008, China; xfwu@pmo.ac.cn

²Guangxi Key Laboratory for Relativistic Astrophysics, Nanning 530004, China

³Instituto de Astrofísica de Andalucía (IAA-CSIC), P.O. Box 03004, E-18080 Granada, Spain

⁴Scientist Support LLC, Madsion, AL 35758, USA

⁵Department of Space Sciences and Astronomy, Hebei Normal University, Shijiazhuang 050024, China

⁶School of Astronomy and Space Science, University of Science and Technology of China, Hefei, Anhui 230026, China

⁷Joint Center for Particle, Nuclear Physics and Cosmology, Nanjing University-Purple Mountain Observatory, Nanjing 210008, China

⁸Department of Astronomy and Astrophysics, Pennsylvania State University, 525 Davey Laboratory, University Park, PA 16802

⁹Department of Physics, Pennsylvania State University, 104 Davey Laboratory, University Park, PA 16802

¹⁰Center for Particle and Gravitational Astrophysics, Institute for Gravitation and the Cosmos, Pennsylvania State University, 525 Davey Laboratory, University Park, PA 16802

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ABSTRACT

Possible violations of Lorentz invariance (LIV) have been investigated for a long time using the observed spectral lags of gamma-ray bursts (GRBs). However, these generally have relied on using a single photon in the highest energy range. Furthermore, the search for LIV lags has been hindered by our ignorance concerning the intrinsic time lag in different energy bands. GRB 160625B, the only burst so far with a well-defined transition from *positive* lags to *negative* lags provides a unique opportunity to put new constraints on LIV. Using multi-photon energy bands we consider the contributions to the observed spectral lag from both the intrinsic time lag and the lag by LIV effects, and assuming the intrinsic time lag to have a positive dependence on the photon energy, we obtain robust limits on LIV by directly fitting the spectral lag data of GRB 160625B. Here we show that these robust limits on the quantum gravity energy scales are $E_{\text{QG},1} \geq 0.5 \times 10^{16}$ GeV for the linear, and $E_{\text{QG},2} \geq 1.4 \times 10^7$ GeV for the quadratic LIV effects, respectively. In addition, we give for the first time a reasonable formulation of the intrinsic energy-dependent time lag.

Subject headings: astroparticle physics — gamma-ray burst: individual (GRB 160625B) — gravitation

1. INTRODUCTION

Spectral lag, the arrival time delay between light curves in different energy bands (or between correlated photons with different energies), is a common feature in gamma-ray bursts (GRBs; e.g., Cheng et al. 1995; Norris et al. 1996; Band 1997). Generally speaking, most GRBs show *positive* lags, i.e., light curves at higher energies (say, in the MeV range) peak earlier than those at lower energies (say, in a range of 10 s to 100 s keV). However, there some rare cases showing zero lags or even *negative* lags (e.g., Norris et al. 2000; Liang et al. 2006; Ukwatta et al. 2012). Since the launch of the *Fermi* satellite, many GRBs with high energy emission above 100 MeV have been detected. In contrast to the *positive* lags of low energy emission, GeV photons are found delayed with respect to MeV photons in many (but not all) GRBs (i.e., *negative* lags; see Abdo et al. 2009a,b; Mészáros & Rees 2011). Some physical models have been formulated to account for the intrinsic origin of lags (e.g., Ioka & Nakamura 2001; Shen et al. 2005; Toma et al. 2009; Uhm & Zhang 2016). Particularly, Uhm & Zhang (2016) showed that the intrinsic *positive* lags could be well reproduced by a simple model invoking synchrotron radiation from a rapidly expanding outflow.

On the other hand, one possible explanation for the *negative* lags is provided by Quantum Gravity (QG) effects. One such effect is the Lorentz invariance violation (LIV). Lorentz invariance is typically expected to be broken at the Planck scale ($E_{\text{QG}} \approx E_{\text{Pl}} = \sqrt{\hbar c^5/G} \simeq 1.22 \times 10^{19}$ GeV; see Mattingly 2005; Amelino-Camelia 2013, and references

therein).¹ Many theories of QG predict that LIV happens at high energy scales, since high energy photons may interact with the foamy structure of space-time at small spatial scales (Amelino-Camelia et al. 1997). In such cases, the speed of light in vacuum would depend on the energy of the photon, and high energy photons propagate in vacuum slower than low energy photons (Amelino-Camelia et al. 1998). The energy scale for LIV, E_{QG} , could therefore be constrained by the arrival time differences of the photons with different energies originating from the same astronomical source (Amelino-Camelia et al. 1998; Ellis & Mavromatos 2013).

Thanks to their short spectral lags, cosmological distances, and very high energetic photons, GRBs have been viewed as the most promising sources for studying the LIV effects (Amelino-Camelia et al. 1998; Ellis et al. 2006; Jacob & Piran 2008). In the past, various limits on LIV have been obtained from the spectral time lags of individual GRB or a large sample of GRBs (e.g., Amelino-Camelia et al. 1998; Coleman & Glashow 1999; Schaefer 1999; Ellis et al. 2003, 2006; Boggs et al. 2004; Kahnashvili et al. 2006; Jacob & Piran 2008; Abdo et al. 2009a,b; Biesiada & Piórkowska 2009; Xiao & Ma 2009; Shao et al. 2010; Chang et al. 2012, 2016; Nemiroff et al. 2012; Ellis & Mavromatos 2013; Kostelecký & Mewes 2013;

¹ Note that here we adopted a LIV scenario with broken relativistic symmetries. This reflects the earlier incarnations of the relevant phenomenology on the QG side, although in recent years more attention has focused on a description of these QG effects in a Doubly Special Relativity (DSR) scenario, in which relativistic symmetries are deformed rather than broken (e.g., Amelino-Camelia 2002a; Amelino-Camelia 2002b; Kowalski-Glikman & Nowak 2002; Magueijo & Smolin 2003).

Vasileiou et al. 2013, 2015; Pan et al. 2015; Zhang & Ma 2015; Wei et al. 2016). In particular, Abdo et al. (2009a) used the time lag of the highest energy (13.2 GeV) photon from GRB 080916C to constrain the linear LIV energy scale ($E_{\text{QG},1}$) and presented a stringent limit of 1.3×10^{18} GeV, improving the previous limits by at least one order of magnitude. Abdo et al. (2009b) set the current strictest limits on both the linear and quadratic LIV energy scales by analyzing the arrival time delay between a 31 GeV photon and the low energy (trigger) photons from GRB 090510. The limits set are $E_{\text{QG},1} > (1-10)E_{\text{Pl}}$ and $E_{\text{QG},2} > 1.3 \times 10^{11}$ GeV. However, these limits were based on the rough time lag of a single GeV-scale photon. It is necessary to consider using the true spectral time lags of bunches of high energy photons (i.e., the lags of high-quality high energy light curves) to constrain the LIV. Furthermore, since the emission mechanism of GRBs is still poorly understood, it is difficult to distinguish an intrinsic time delay at the source from a delay induced by propagation in vacuum to the observer. That is, the method of the flight-time difference used for testing LIV is hindered by our ignorance concerning the intrinsic time delay in different energy bands (see, e.g., Ellis et al. 2006; Biesiada & Piórkowska 2009).

The first attempt to disentangle the intrinsic time delay problem was presented in Ellis et al. (2006). They proposed to work on statistical samples of GRBs at a range of different redshifts, and formulated the problem in terms of a linear regression analysis where the slope corresponds to the QG scale related to the LIV effect, and the intercept represents the possible intrinsic time delay. This analysis has the advantage that it can extract the spectral time lags of broad light curves in different energy bands. In this manner, a weak evidence for LIV was found under the assumption that all GRBs had the same intrinsic time delay (Ellis et al. 2006). However, due to the fact that the durations of GRBs span about six orders of magnitude, it is not likely that the high energy photons emitted from different GRBs (or from the same GRB) have the same intrinsic time lag as compared with the emission time of the low energy photons (Chang et al. 2016). As an improvement, Zhang & Ma (2015) fitted the data of the energetic photons from GRBs on straight lines with the same slope but with different intercepts (i.e., different intrinsic time lags). Unfortunately, photons from different GRBs on the same line still mean that the intrinsic time lags between the high energy photons and the onset low energy photons are approximately the same for these GRBs, which is not always true and it could be a coincidence. Chang et al. (2012) estimated the intrinsic time lag between emissions of high and low energy photons from GRBs by using the magnetic jet model. However, the magnetic jet model relies on some particular theoretical parameters, and this leads to uncertainties on the LIV results.

Recently, *Fermi* detected a peculiar burst GRB 160625B, which had three dramatically different isolated sub-bursts (Burns 2016), with unusually high photon statistics allowing the use of amply populated energy bands. Here we calculate the spectral lags between the lowest energy band (10–12 keV) and any other high energy band for the second sub-burst of GRB 160625B, and find that the lag increases at $E \lesssim 8$ MeV, and then shows a steep decline in the energy range $8 \text{ MeV} \lesssim E \lesssim 20 \text{ MeV}$. In other words, the behavior of the spectral lags of this GRB is quite different, and a transition from *positive* lags to *negative* lags is, for the first time, discovered within a burst. If the LIV effect which happens at

high energy scales is considered here, the observed time lag (Δt_{obs}) between different energy bands of a GRB should consist of two terms

$$\Delta t_{\text{obs}} = \Delta t_{\text{int}} + \Delta t_{\text{LIV}}, \quad (1)$$

where Δt_{int} represents the intrinsic emission time delay, and Δt_{LIV} denotes the time delay induced by the LIV effect. Instead of assuming an unknown constant for Δt_{int} , we argue that the intrinsic lag should be positively correlated with the energy, i.e., the higher-energy photon arrives earlier than the lower-energy photon (Shao et al. 2016). Due to the LIV effect at high energy scales, a high-energy photon emitted (ideally) simultaneously with a low energy photon is to be observed later than that low-energy photon. Here we study the LIV effect of the high energy photons in this direction. Put differently, Δt_{int} and Δt_{LIV} have a different sign and, therefore, this positive correlation between the lag and the energy gradually becomes an anti-correlation.

In this work, we develop a new method through which a reasonable formulation of the intrinsic time delay can be derived, by fitting the energy dependence of the time lag. This allows us simultaneously to obtain robust limits on the 1st order and 2nd order QG energy scale. We describe the data analysis in Section 2, and our methods and results are presented in Section 3. Our conclusions are briefly summarized in Section 4.

2. THE OBSERVED PROPERTIES OF SPECTRAL LAGS OF GRB 160625B

At $T_0 = 22 : 40 : 16.28$ UT on 2016 June 25, the *Fermi* Gamma-Ray Burst Monitor (GBM; Burns 2016) triggered and located GRB 160625B for the first time. Then the *Fermi* Large Area Telescope (LAT; Dirirsa et al. 2016) detected a sharp increase in the rate of high-energy photons at 22:43:24.82 UT, resulting in an onboard trigger on a bright pulse from the same GRB. At 22:51:16.03 UT, GBM triggered again on GRB 160625B (Burns 2016). The gamma-ray light curve of GRB 160625B consists of three dramatically different isolated sub-bursts with a total duration of about $T_{90} = 770$ s (15–350 keV; Zhang et al. 2016). The first sub-burst (precursor) that initially triggered the GBM is soft with a duration of about 0.84 s. The precursor is followed, corresponding to the LAT trigger and starting at $\sim T_0 + 180$ s, by the main, extremely bright and spectrally-hard episode with a duration of about 35.10 s. After a long waiting time (~ 339 s), the third sub-burst trigger GBM again which has a duration of about 212.22 s. Spectroscopic observations reveals absorption features consistent with Mg I, Mg II, Mn II and Fe II lines at a redshift of $z = 1.41$ (Xu et al. 2016).

Since the second sub-burst of GRB 160625B is very bright, we can easily extract its light curves in different energy bands (see Figure 1). In this analysis, we use the cross-correlation function (CCF) method to calculate the lags between light curves of different energies for intervals 180.6–215.7 s of the burst. The detailed CCF method is described in Zhang et al. (2012). We look for spectral time lags in the light curves recorded in the lowest energy band (10–12 keV) relative to any other GBM light curves with higher energy bands, and find that the lag behavior is quite different. A transition from *positive* lags to *negative* lags is first discovered at $E \sim 8$ MeV (see Figure 2). The observed time lags we extract from the energy-dependent light curves are listed in Table 1, together with their energy bands.

3. CONSTRAINTS ON THE VIOLATION OF LORENTZ INVARIANCE

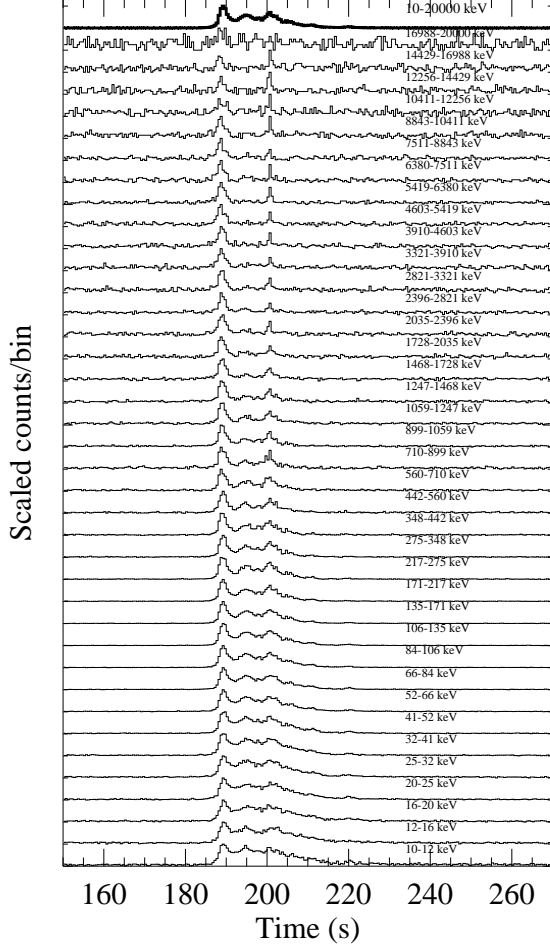


FIG. 1.— Energy-dependent light curves of the second sub-burst of GRB 160625B. The full-range (10–20000 keV) light curve is shown on top (thick black line).

TABLE 1
THE TIME LAGS BETWEEN THE LOWEST ENERGY BAND (10–12 keV) AND ANY OTHER HIGH ENERGY BANDS FOR THE SECOND SUB-BURST OF GRB 160625B

Energy (keV)	Δt_{obs} (s)	Energy (keV)	Δt_{obs} (s)
12–16	-0.070 ± 0.134	1059–1247	1.892 ± 0.158
16–20	-0.015 ± 0.130	1247–1468	2.208 ± 0.162
20–25	0.081 ± 0.125	1468–1728	2.375 ± 0.179
25–32	0.210 ± 0.123	1728–2035	2.088 ± 0.193
32–41	0.296 ± 0.124	2035–2396	2.361 ± 0.208
41–52	0.466 ± 0.122	2396–2821	2.325 ± 0.212
52–66	0.611 ± 0.127	2821–3321	2.242 ± 0.255
66–84	0.699 ± 0.122	3321–3910	2.334 ± 0.273
84–106	0.913 ± 0.120	3910–4603	3.080 ± 0.290
106–135	1.012 ± 0.128	4603–5419	3.538 ± 0.382
135–171	1.204 ± 0.121	5419–6380	4.306 ± 0.409
171–217	1.257 ± 0.132	6380–7511	4.142 ± 0.483
217–275	1.290 ± 0.131	7511–8843	4.435 ± 0.542
275–348	1.477 ± 0.145	8843–10411	2.681 ± 0.653
348–442	1.908 ± 0.168	10411–12256	1.670 ± 0.803
442–560	1.846 ± 0.182	12256–14429	1.962 ± 0.906
560–710	1.856 ± 0.202	14429–16988	-0.223 ± 1.030
710–899	2.765 ± 0.243	16988–20000	1.637 ± 0.858
899–1059	2.079 ± 0.143		

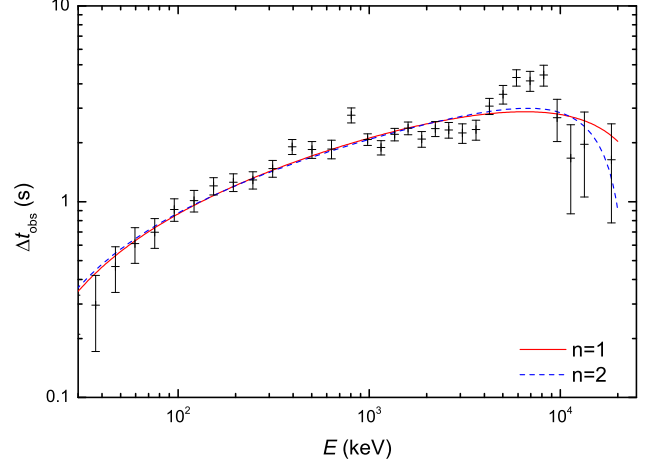


FIG. 2.— Energy dependence of the observed spectral lag Δt_{obs} (relative to the softest band), and the best-fit theoretical curves: (solid line) the linear ($n = 1$) LIV model; (dashed line) the quadratic ($n = 2$) LIV model.

As mentioned above, the LIV-induced time lag Δt_{LIV} may be accompanied by an unknown intrinsic energy-dependent time lag Δt_{int} caused by the unknown emission mechanism of GRBs. Here we propose, for the first time, that the contributions of both the intrinsic time lag and the LIV effects can result in a lag behavior with a transition from *positive* lags to *negative* lags. Due to the fact that the dominant fraction of GRB light curves show *positive* lags (e.g., [Shao et al. 2016](#)), we suggest that there is a positive correlation between the intrinsic time lag and the energy. As the LIV effect takes the lead at the high energy scales, this positive correlation trends in an opposite way.

3.1. The intrinsic energy-dependent Time Lag

In the observer frame, we assume the intrinsic positive time lag (between the lowest energy band and any other high energy bands) increases with the energy E in the form of an approximate power-law function:

$$\Delta t_{\text{int}}(E) = \tau \left[\left(\frac{E}{\text{keV}} \right)^\alpha - \left(\frac{E_0}{\text{keV}} \right)^\alpha \right] \text{ s}, \quad (2)$$

with $\tau > 0$ and $\alpha > 0$, where $E_0 = 11.34$ keV is the median value of the fixed lowest energy band (10–12 keV). The coefficient τ and the index α are free parameters, which must be optimized simultaneously with the QG energy scale E_{QG} (more on this below). We emphasize that a *positive* lag corresponds to an earlier arrival time for the higher energy emission in this study.

3.2. The time delay induced by the LIV effect

In QG scenarios, the LIV induced modifications to the photon dispersion relation can be expressed by the leading term of the Taylor expansion as

$$E^2 \simeq p^2 c^2 \left[1 - s_{\pm} \left(\frac{pc}{E_{\text{QG},n}} \right)^n \right], \quad (3)$$

which corresponds to a photon propagation speed

$$v = \frac{\partial E}{\partial p} \approx c \left[1 - s_{\pm} \frac{n+1}{2} \left(\frac{E}{E_{\text{QG},n}} \right)^n \right], \quad (4)$$

where E_{QG} denotes the QG energy scale, the n -th order expansion of the leading term corresponds to the linear ($n = 1$) or quadratic ($n = 2$ order), and $s_{\pm} = \pm 1$ is the “sign” of the LIV effect ($s_{\pm} = +1$ or $s_{\pm} = -1$ stands for a decrease or an increase in photon velocity with an increasing photon energy). In the case of $s_{\pm} = +1$, photons with higher energies would travel slower than those with lower energies in vacuum. This predicts a *negative* spectral lag due to LIV, so we consider the $s_{\pm} = +1$ case in the following.

Because of the energy dependence of the photon speed, two photons with different energies (denoted by E and E_0 , where $E > E_0$) emitted simultaneously from the same source would arrive on Earth at different times. Taking into account the cosmological expansion, the LIV induced time delay is given by (Jacob & Piran 2008; Zhang & Ma 2015)

$$\begin{aligned} \Delta t_{LIV} &= t_l - t_h \\ &= -\frac{1+n}{2H_0} \frac{E^n - E_0^n}{E_{QG,n}^n} \int_0^z \frac{(1+z')^n dz'}{\sqrt{\Omega_m(1+z')^3 + \Omega_\Lambda}}, \end{aligned} \quad (5)$$

where t_l and t_h are the arrival times of the low energy photon and the high energy photon, respectively. Here we use the cosmological parameters determined by the *Planck* observations (Planck Collaboration et al. 2014): $H_0 = 67.3 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_m = 0.315$, and $\Omega_\Lambda = 1 - \Omega_m$.

3.3. Results

With the 37 lag–energy measurements (see Table 1 and Figure 2), from Equations (1, 2, and 5), we perform a global fitting to determine the free parameters (τ , α , and E_{QG}) simultaneously using the Monte Carlo (MC) approach. A fitting engine (*McFit*) has been developed, which employs a Bayesian MC fitting technique to realistically fit free parameters that are constrained by the observed data even when other parameters are unconstrained. With the help of this technique, the best-fit parameters and their uncertainties can be reliably determined by the converged MC chains.

We first fit the observed lag–energy data with the linear LIV case (i.e., $n = 1$). The resulting constraints on τ , α , and $E_{QG,1}$ are shown in Figure 3. These contours show that at the 1σ level, the best-fit parameter values are $\tau = 1.20^{+2.71}_{-0.04} \text{ s}$, $\alpha = 0.18^{+0.01}_{-0.10}$, and $\log(E_{QG,1}/\text{GeV}) = 15.66^{+0.55}_{-0.01}$, with a $\chi^2_{\text{dof}} = 81.22/34 = 2.39$.

Next, we consider the quadratic LIV case (i.e., $n = 2$) to fit the observed lag–energy data. The parameter constraints are displayed in Figure 4. We see here that the best-fit corresponds to $\tau = 2.18^{+2.90}_{-0.31} \text{ s}$, $\alpha = 0.12^{+0.01}_{-0.05}$, and $\log(E_{QG,2}/\text{GeV}) = 7.17^{+0.17}_{-0.02}$. With $37 - 3 = 34$ degrees of freedom, we have $\chi^2_{\text{dof}} = 76.59/34 = 2.25$.

The best-fitting theoretical curves for the linear LIV case (solid line; with $\tau = 1.20 \text{ s}$, $\alpha = 0.18$, and $\log(E_{QG,1}/\text{GeV}) = 15.66$) and for the quadratic LIV case (dashed line; with $\tau = 2.18 \text{ s}$, $\alpha = 0.12$, and $\log(E_{QG,2}/\text{GeV}) = 7.17$) are shown in Figure 2. This reveals that both cases are adequate to represent the data.

With the best-fit values of $\log E_{QG,1}$ and $\log E_{QG,2}$ as well as their 1σ error bars, the 1σ confidence-level lower limit on LIV is

$$E_{QG,1} \geq 0.5 \times 10^{16} \text{ GeV} \quad (6)$$

for the linear ($n = 1$) LIV case, and

$$E_{QG,2} \geq 1.4 \times 10^7 \text{ GeV} \quad (7)$$

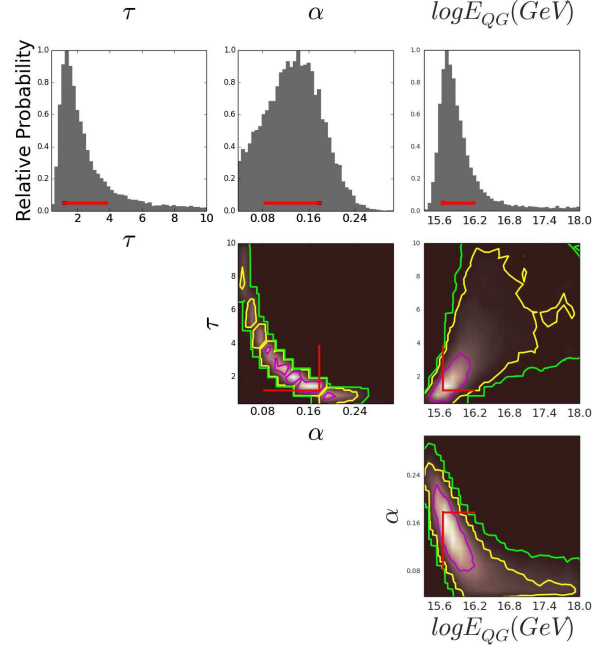


FIG. 3.— Parameter constraints of the linear ($n = 1$) LIV case fitting for the lag–energy data. Histograms and contours display the likelihood map of the parameter-constraint outputs by our *McFit* package. Red crosses indicate the best-fit values and their 1σ error bars.

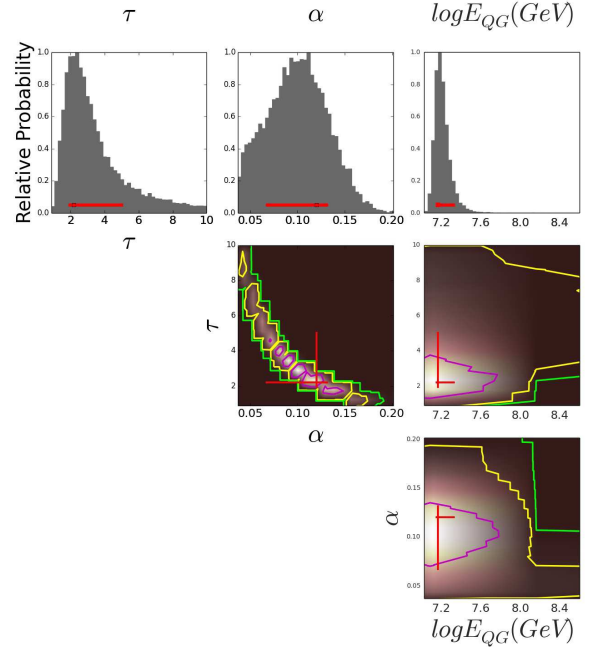


FIG. 4.— Same as Figure 3, except now for the quadratic ($n=2$) LIV case.

3.4. Other possible LIV tests

There are some observations (e.g, the ultrahigh energy cosmic rays and the TeV photons) with energies above an expected threshold (pion production or pair creation), which can be considered as “threshold anomalies”. It has been proposed that LIV could be the origin of the threshold anomalies (Amelino-Camelia & Piran 2001). That is, the LIV scenario could be tested not only by the study of spectral lags but also

by analysis of data on such threshold anomalies. The limits on LIV from the threshold anomalies are at a level well beyond the sensitivity of the analysis reported in this paper (see Mattingly 2005; Amelino-Camelia 2013, and references therein). On the other hand, it is well known that threshold anomalies do not apply to the DSR scenario (see Mattingly 2005; Amelino-Camelia 2013). These results on threshold anomalies would imply that the analysis of spectral lags reported in this paper would not carry much weight on the debate concerning LIV (since more stringent limits may be established via the threshold anomalies), being instead a more valuable contribution to the debate on the DSR scenario.

4. SUMMARY AND DISCUSSION

The observed spectral lags of GRBs have been widely used to constrain the energy scales of LIV. The key issue in the idea of searching for spectral lags, however, is to distinguish the possible time delay induced by the LIV effect from any source-intrinsic time lag in the emission of photons at different energies. In order to overcome the intrinsic time lag problem, Ellis et al. (2006) proposed a data fitting procedure to test the LIV effect, and an unknown constant was assumed to be the intrinsic time lag in the linear fitting function, and furthermore assuming that all GRBs have the same intrinsic time lag.

Here, instead of assuming an unknown constant for the intrinsic time lag, we argue that the intrinsic lag has a positive dependence on the photon energy. On the other hand, the LIV effects which are expected at high energy scales would make high energy photons travel in vacuum slower than low energy photons, so we suggest that the positive correlation between the lag and the energy will gradually become an anti-correlation at the high energy scales. In this work, we successfully fit the evolving behavior of the spectral lags of GRB 160625B (i.e., the existence of a transition from *positive* lags to *negative* lags), by considering the contributions of both the intrinsic time lag and the lag by the LIV effect. This is the first time, to our knowledge, that it has been possible to give both a reasonable formulation of the intrinsic energy-dependent time lags and robust limits on LIV through direct fitting of the spectral lag data of a GRB.

Our limit on the linear LIV case ($E_{\text{QG},1} \geq 0.5 \times 10^{16}$ GeV) obtained here from the spectral lags is comparable to the limit found from Ellis et al. (2006) with an unknown constant for the intrinsic time lag, being less than three orders of magnitude below the Planck energy scale. Our limit on the quadratic

LIV case ($E_{\text{QG},2} \geq 1.4 \times 10^7$ GeV) is four orders of magnitude below the current best limit from the single GeV photon of GRB 090510 (Abdo et al. 2009b; Vasileiou et al. 2013). While the spectral lags of GRB 160625B do not currently have the best sensitivity to LIV constraints, there is nonetheless merit to the result. Firstly, because the true spectral time lags of broad light curves in different energy multi-photon bands are used to obtain reliable constraints on LIV, rather than the rough time lags obtained from a single GeV photon. Secondly, because the analysis of the intrinsic time lag performed here is important for studying the flight time differences from the astronomical sources to test the LIV effect, since it impacts the reliability of the resulting constraints on LIV. Compared with previous works, the problems associated with the intrinsic time lags can be obviously handled better with our new method. Furthermore, it is reasonable to expect that GRB 160625B is not the only burst where a transition from *positive* to *negative* lags can be determined, and the method presented here can be used for any burst with similar lag features. More stringent constraints on LIV can be expected as our method is applied to larger numbers of GRBs with higher temporal resolutions and more high energy photons.

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